

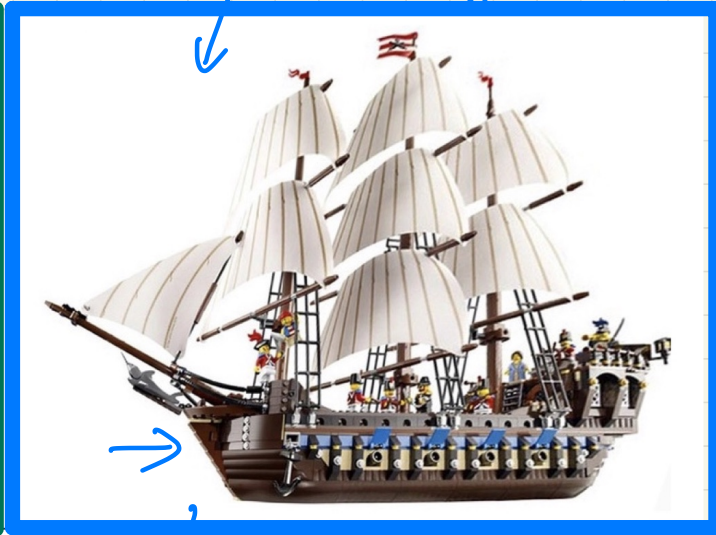
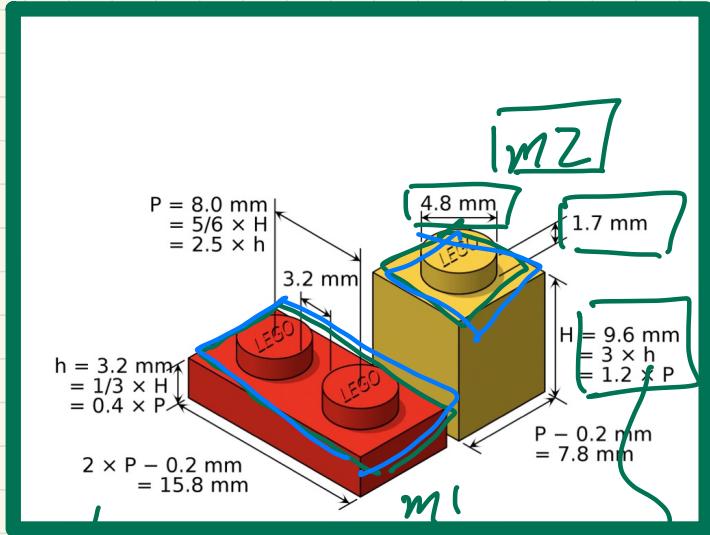
## Lecture 2

### Part 1

# ***Modularity & Modular Design Abstract Data Types (ADTs)***

# Modularity: Childhood Activities

assembly of modules.

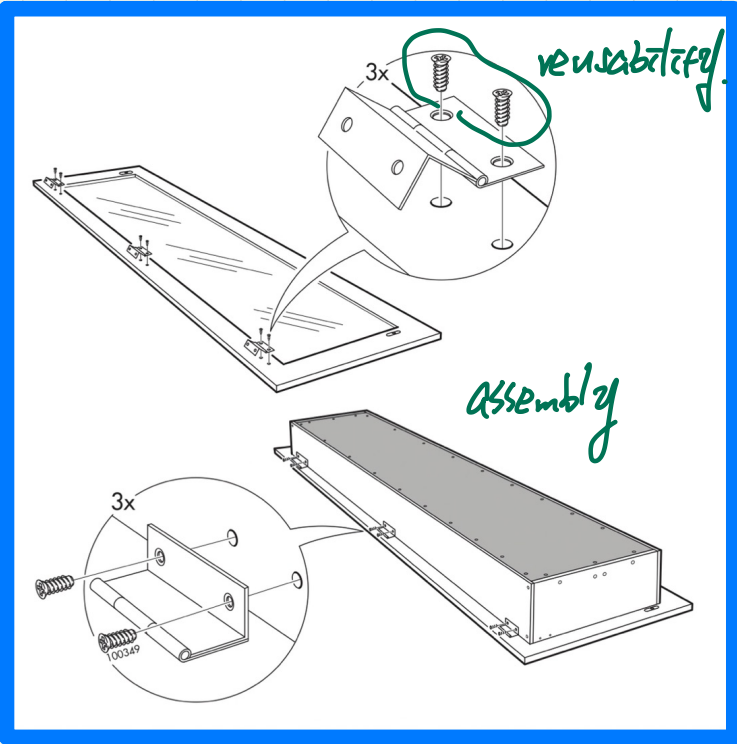
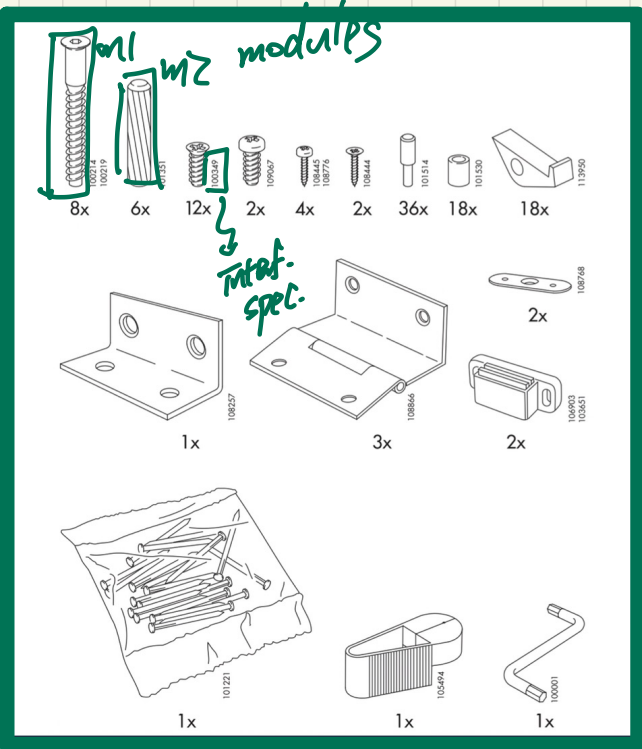


modules

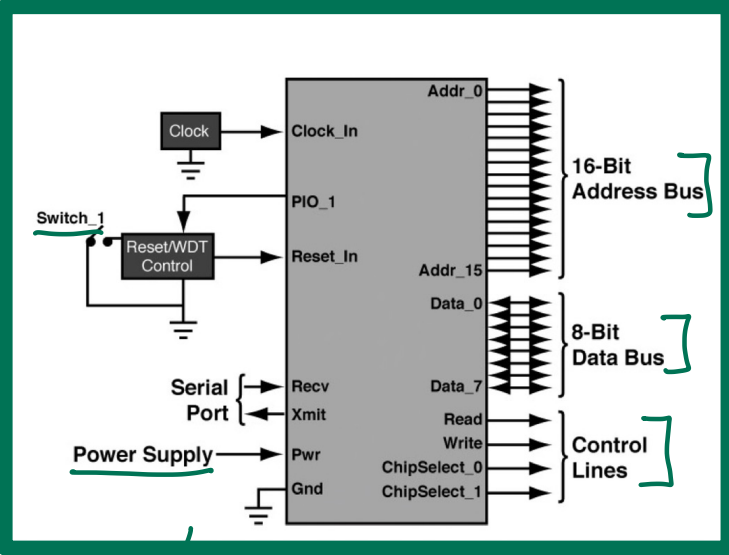
interface specification

reusable

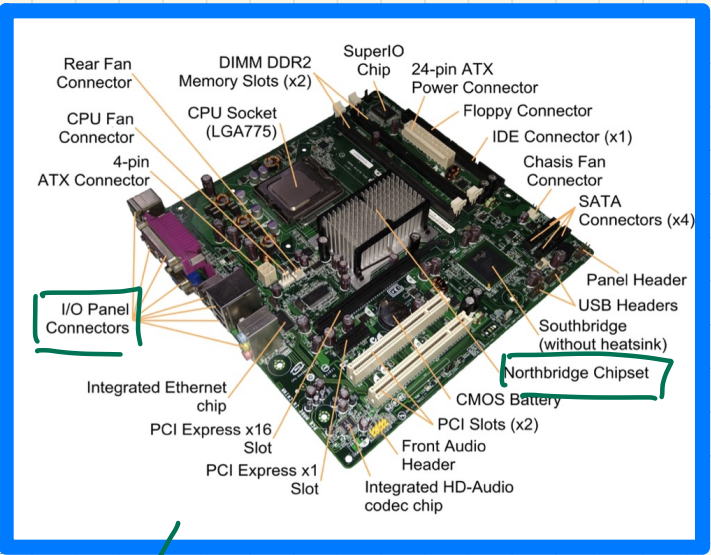
# Modularity: Daily Constructions



# Modularity: Computer Architectures

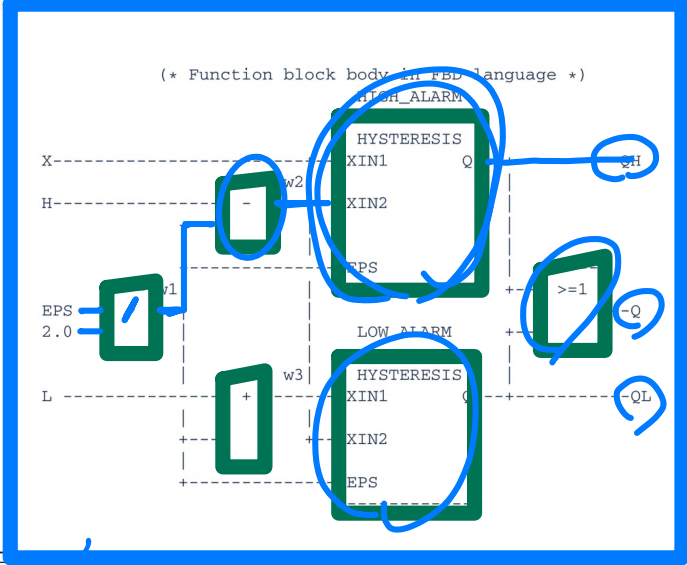
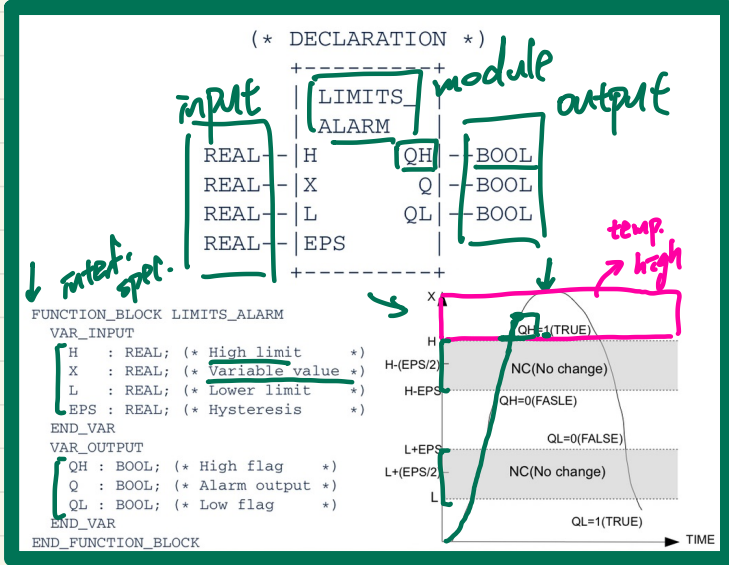


spec.

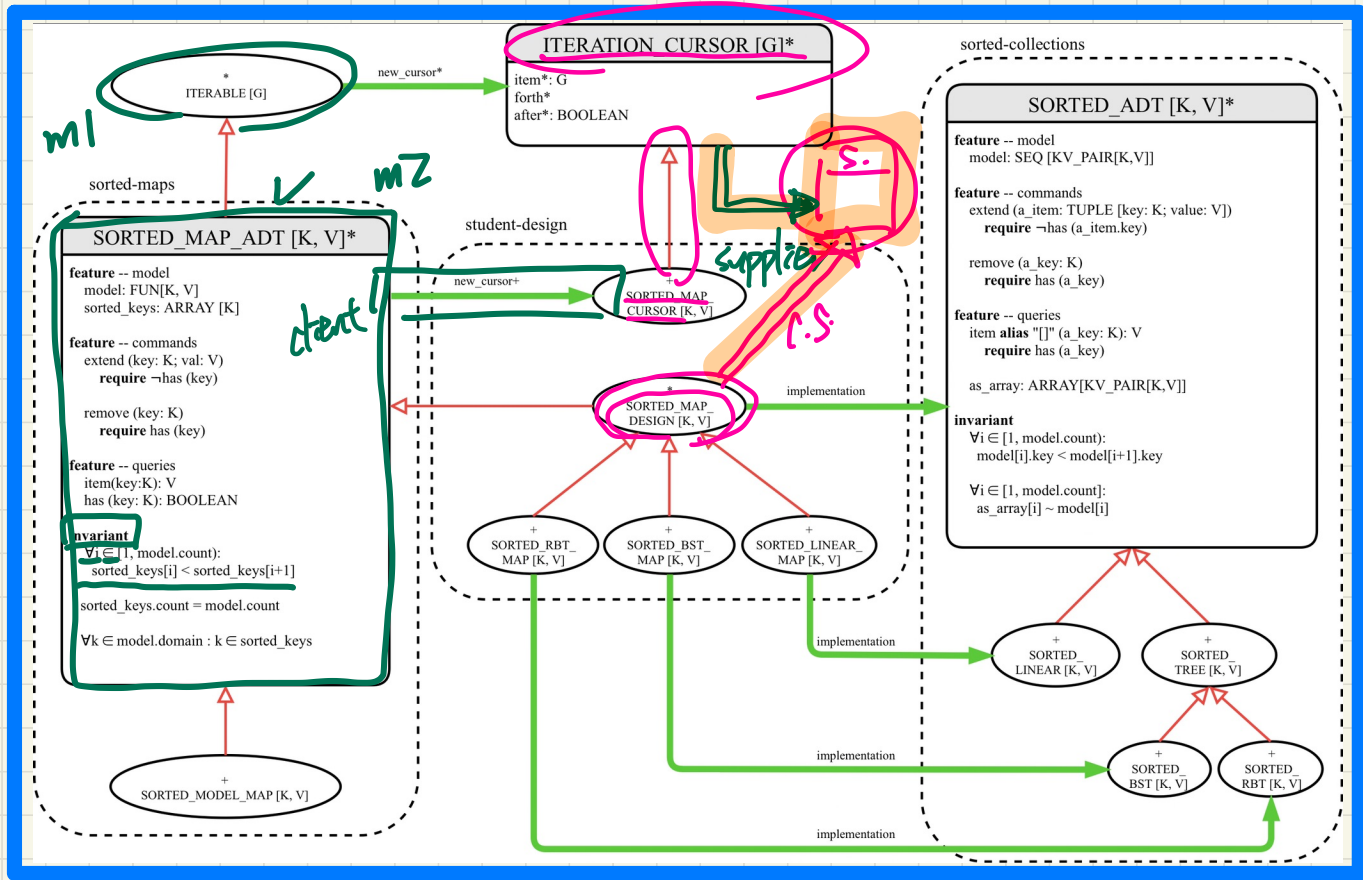


assembly.

# Modularity: System Developments



# Modularity: Software Design



# Java Classes: Abstract Data Types? No.

**set**(int index, E element)  
Replaces the element at the specified position in this list with the specified element (optional operation).


**set**  
E set(int index, E element)

Replaces the element at the specified position in this list with the specified element (optional operation).

**Parameters:**  
index - index of the element to replace  
element - element to be stored at the specified position

**Returns:**  
the element previously at the specified position

**Throws:**  
UnsupportedOperationException - if the set operation is not supported by this list  
ClassCastException - if the class of the specified element prevents it from being added to this list  
NullPointerException - if the specified element is null and this list does not permit null elements  
IllegalArgumentException - if some property of the specified element prevents it from being added to this list  
IndexOutOfBoundsException - if the index is out of range (index < 0 || index >= size())



gen. param.

## Interface List<E>

### Type Parameters:

E - the type of elements in this list

### All Superinterfaces:

Collection<E>, Iterable<E>

### All Known Implementing Classes:

AbstractList, AbstractSequentialList, ArrayList, AttributeList, CopyOnWriteArrayList, LinkedList, RoleList, RoleUnresolvedList, Stack, Vector

```
public interface List<E>  
    extends Collection<E>
```

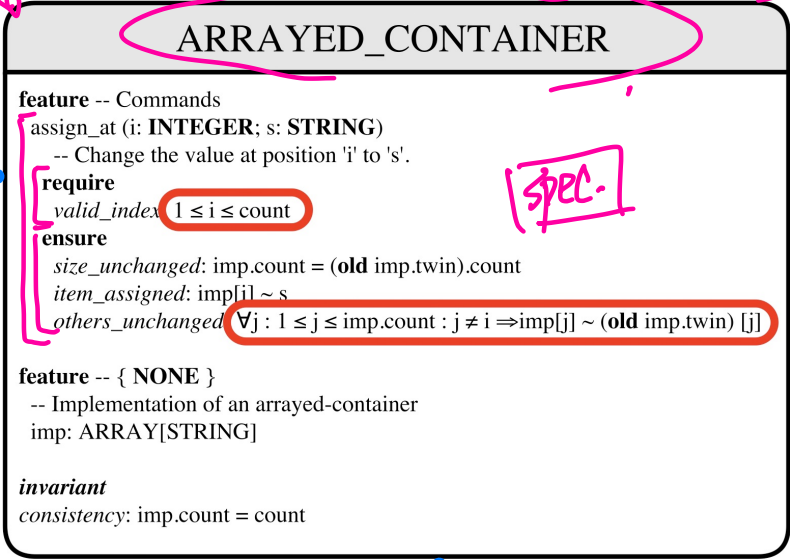
An ordered collection (also known as a *sequence*). The user of this interface has precise control over where in the list each element is inserted. The user can access elements by their integer index (position in the list), and search for elements in the list.

# Eiffel Classes: Abstract Data Types?

## Design Diagram

### Contract View

```
class interface ARRAYED_CONTAINER
feature -- Commands
  assign_at (i: INTEGER; s: STRING)
    -- Change the value at position 'i'
  require
    valid_index: 1 <= i and i <= count
  ensure
    size_unchanged:
      imp.count = (old imp.twin).count
    item_assigned:
      imp [i] ~ s
    others_unchanged:
      across
        1 .. imp.count as j
        all
          j.item /= i implies imp [j.item] ~ (old imp.twin) [j.item]
        end
  count: INTEGER
invariant
  consistency: imp.count = count
end -- class ARRAYED_CONTAINER
```



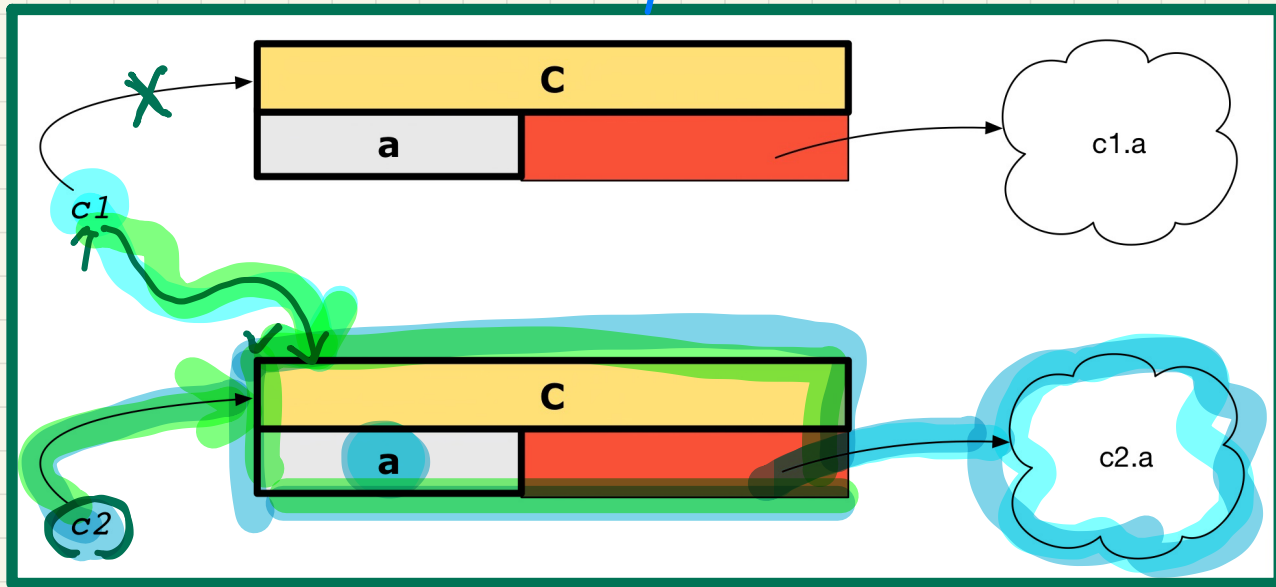


## Lecture 2

### Part 2

# ***Copying Objects: Reference vs. Shallow vs. Deep***

Reference Copy:  $c1 := c2$  ref. copy  
 ↳ cheap ref. copy



$\text{c1} = \text{c2}$  (T)  
 ↳ equality

c1.a = c2.a (T)





# Reference vs. Shallow vs. Deep Copies

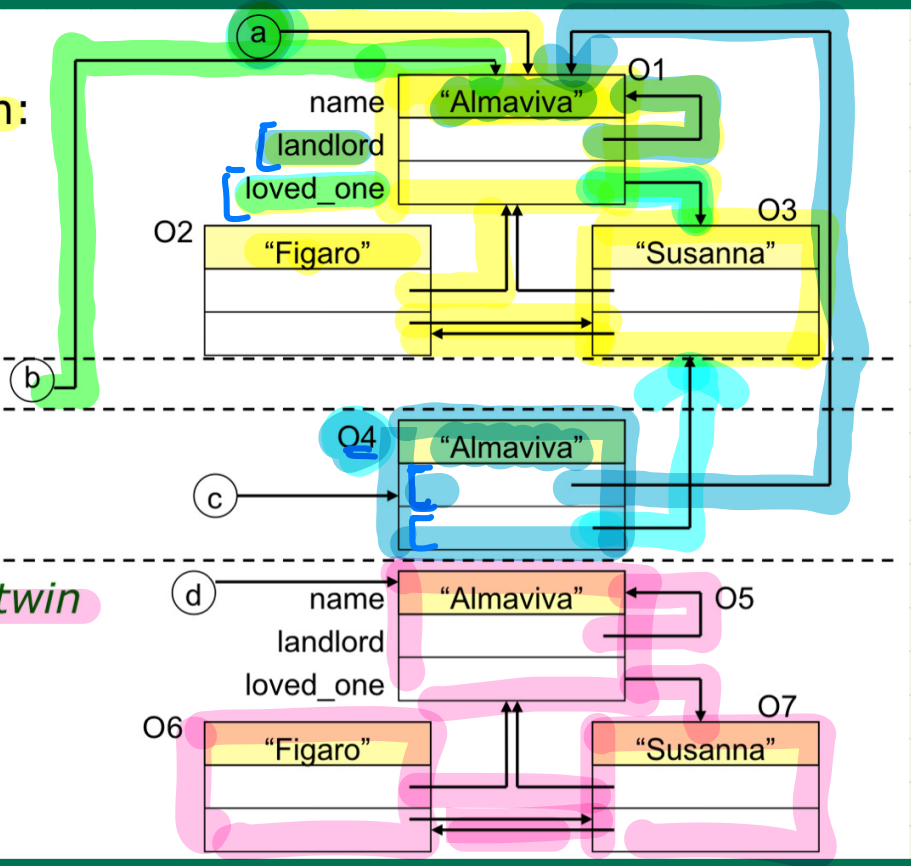
Initial situation:

Result of:

$b := a$

$c := a.twin$

$d := a.deep\_twin$



$O4.l_d := a.l_d$   
 $O4.l_o := a.l_o$

# Collection Objects: Reference Copy & Make Changes

```

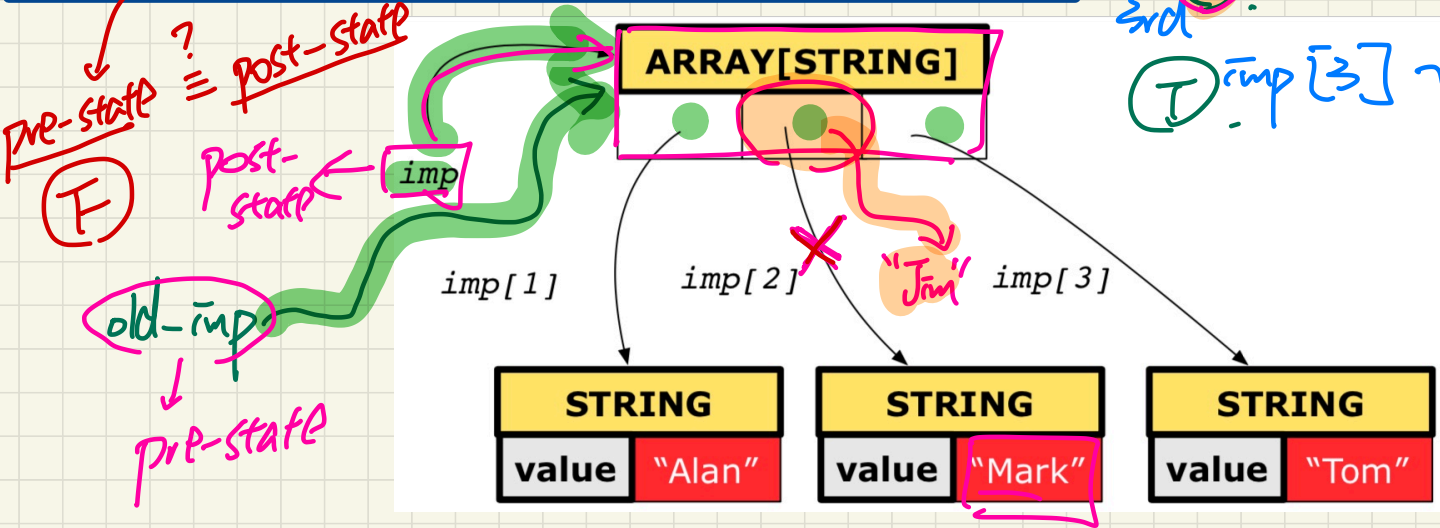
1  old_imp := imp Ref.
2  Result := old_imp = imp -- Result = true
3  imp[2] := "Jim" change. post-staff
4  Result :=
5  across 1 |...| imp.count is j
6  all imp [j] ~ old_imp [j]
7  end -- Result = true
    
```

inappropriate for us to see the change.

1st  $imp[1] \sim old\_imp[1]$

2nd  $imp[2] \sim old\_imp[2]$

3rd  $imp[3] \sim old\_imp[3]$



# Collection Objects: Shallow Copy & Make 1st-Level Changes

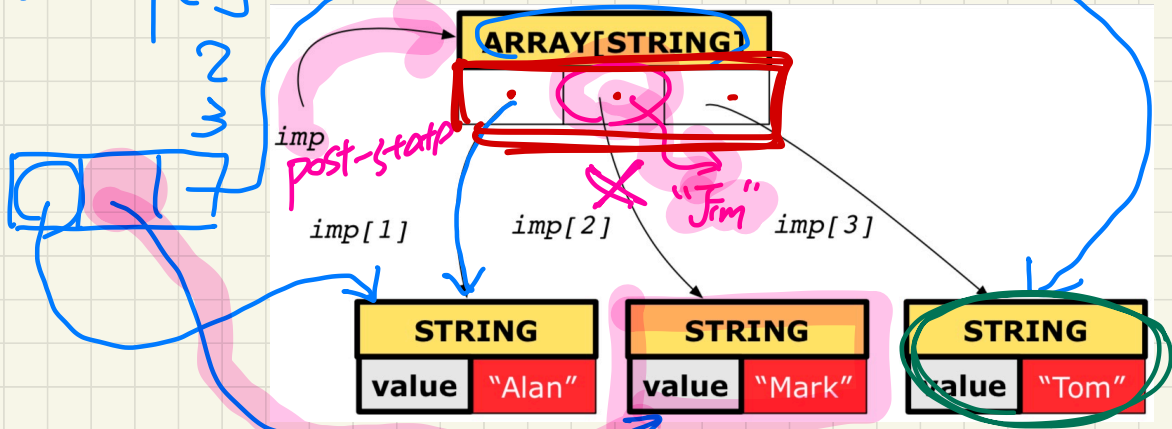
```

1  old_imp := imp.twin shallow
2  Result := old_imp = imp -- Result = false
3  imp[2] := "Jim"
4  Result :=
5  across 1 |..| imp.count is j
6  all imp [j] ~ old_imp [j]
7  end -- Result = false
    
```

1st  $\textcircled{T}$  appropriate to set there's a change  
 $\text{imp}[1] \sim \text{old\_imp}[1]$   
 2nd  $\textcircled{F}$   $\text{imp}[2] \sim \text{old\_imp}[2]$  post-state pre-state  
 3rd  $\textcircled{T}$   $\text{imp}[3] \sim \text{old\_imp}[3]$

$\textcircled{F}$  pre-state  
 ||  
 post-state

$\text{dd\_imp}[1] := \text{imp}[1]$   
 2  
 3  
old\_imp  
 pre-state.



# Collection Objects: Shallow Copy & Make 2nd-Level Changes

```

1  old_imp := imp.twin
2  Result := old_imp = imp -- Result = false
3  imp[2].append("***")
4  Result :=
5  across 1 |..| imp.count is j
6  all imp [j] ~ old_imp [j]
7  end -- Result = true
    
```

to sep the change.

1st  $\text{imp}[1] \sim \text{old\_imp}[1]$

2nd  $\text{imp}[2] \sim \text{old\_imp}[2]$

3rd  $\text{imp}[3] \sim \text{old\_imp}[3]$

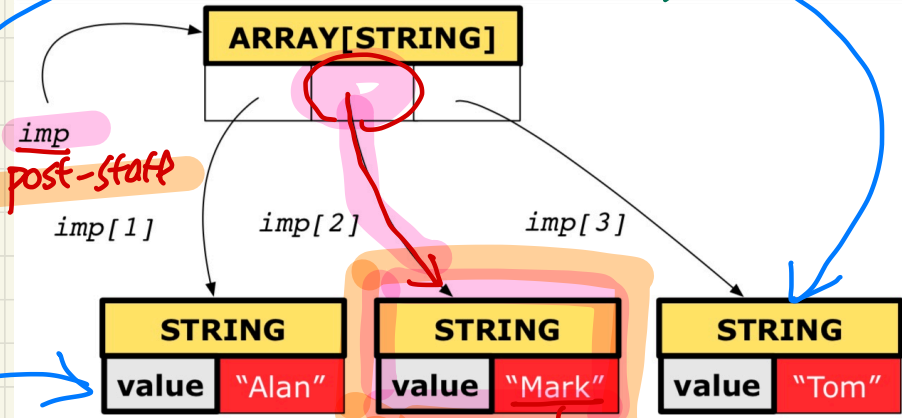
inappropriate

pre-staff

post-staff

(pre-staff)

old\_imp



Mark \* \* \* \*



# Collection Objects: Deep Copy & Make 1st-Level Changes

```

1  old_imp := imp deep_twin
2  Result := old_imp = imp -- Result = false
3  imp[2] := "Jim"
4  Result :=
5    across 1 |..| imp.count is j
6    all imp [j] ~ old_imp [j] end -- Result = false
    
```

appropriate

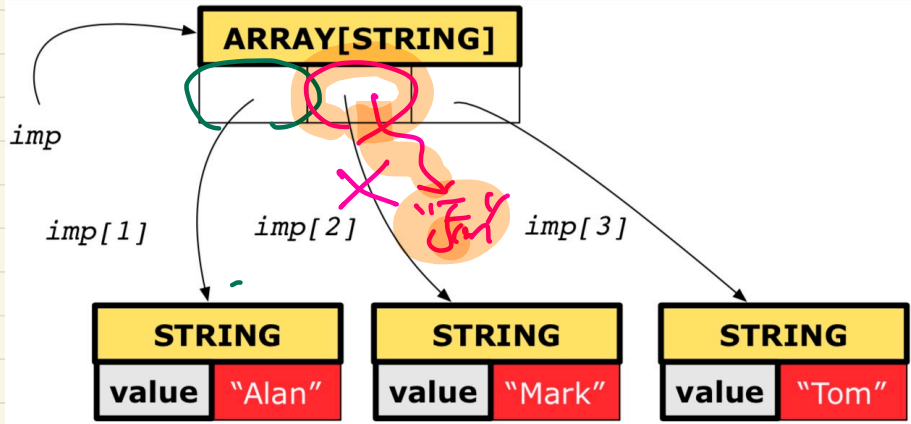
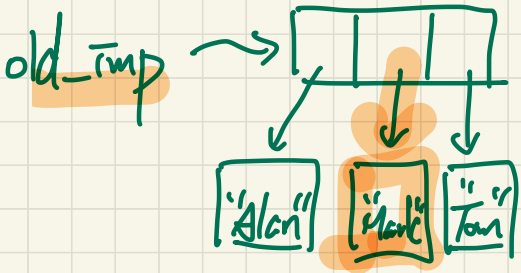
1st (T) .  
 $imp[i] \sim old\_imp[i]$

2nd (F) .  
 $imp[2] \sim old\_imp[2]$

3rd (T) .  
 $imp[3] \sim old\_imp[3]$

pre-staff (F)  
 post-staff

$old\_imp[i] := imp[i].deep\_twin$



# Collection Objects: Deep Copy & Make 2nd-Level Changes

```

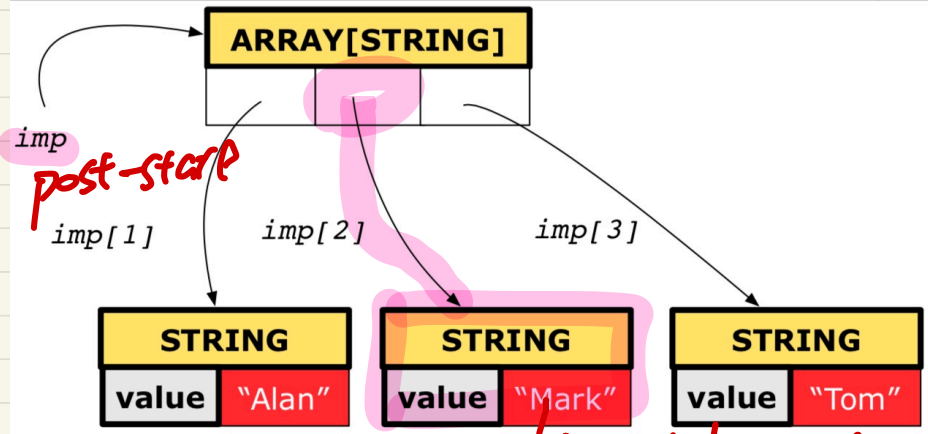
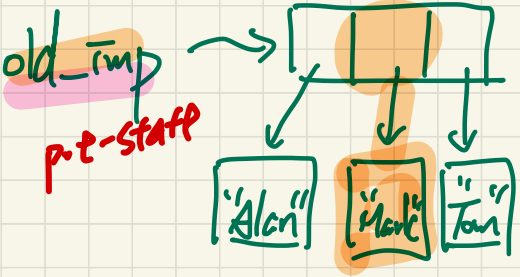
1  old_imp := imp.deep_twin
2  Result := old_imp = imp  -- Result = 
3  imp[2].append ("***")
4  Result :=
5  across 1 |..| imp.count is j
6  all imp [j] ~ old_imp [j] end  -- Result = false

```

Appropriat

pre-staff (F)  
post-staff

1st (T)  
imp[1] ~ old\_imp[1]  
2nd (F)  
imp[2] ~ old\_imp[2]  
3rd (T)  
imp[3] ~ old\_imp[3]



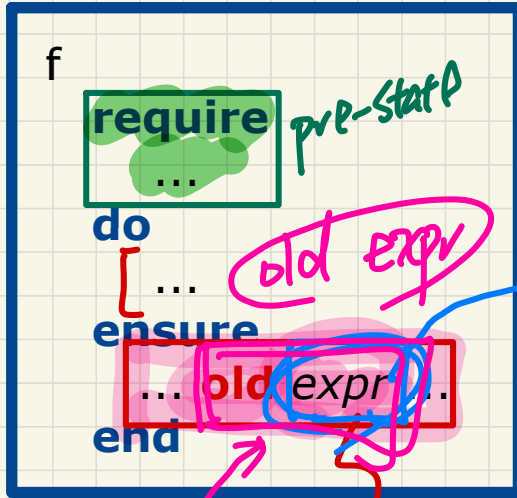
Mark\*\*\*

## Lecture 2

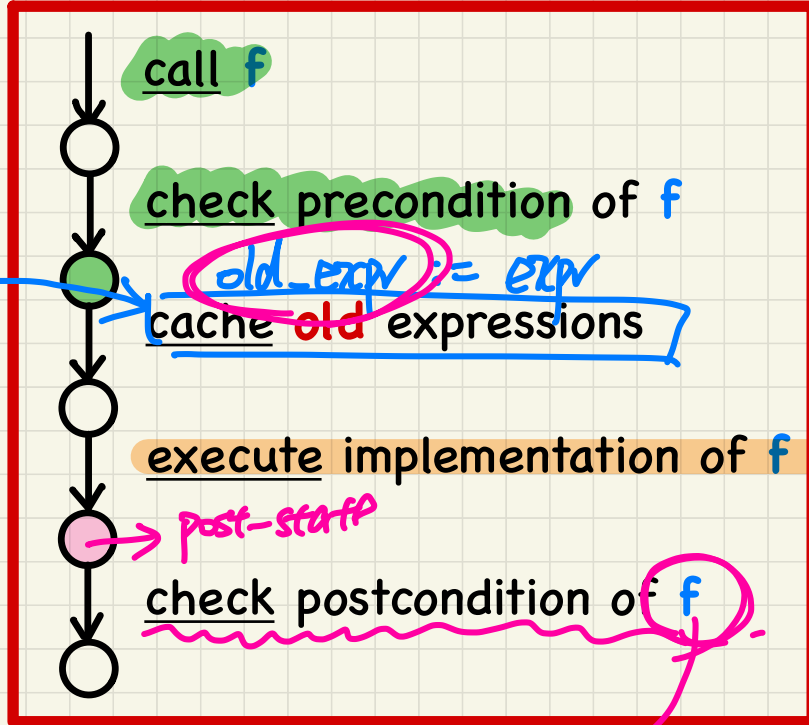
### Part 3

# ***Writing Complete Postconditions***

## Contract View



## Runtime Contract Checks



# Caching Values for **old** Expressions in Postconditions

```
class BANK  
  accounts: ARRAY [ACCOUNT]
```

```
  some_feature
```

```
  [require
```

```
  do ... cache old exp.
```

```
  ensure
```

```
  ... old expr ..
```

```
  end
```

```
end
```

*Current  
accounts  
accounts[i]*

*accounts[i].id*



```
class ACCOUNT  
  id: INTEGER  
end
```

# Caching Values for **old** Expressions in Postconditions

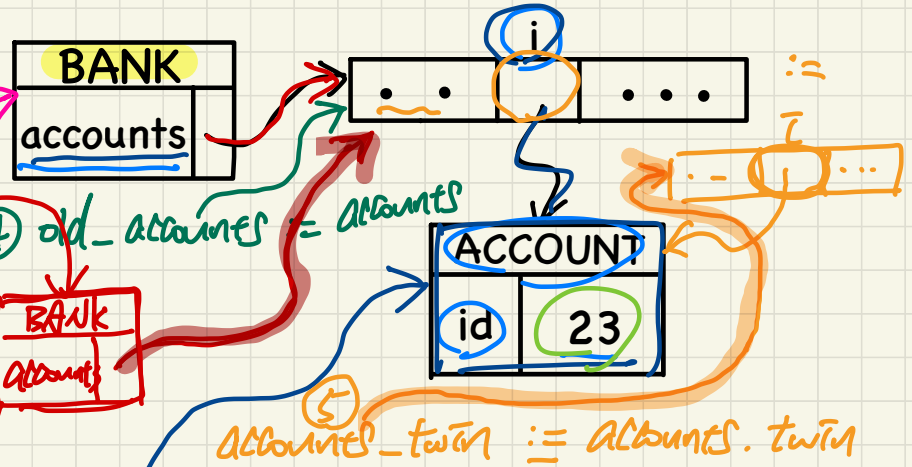
Lecture I  
 ↳ TBC Java  
 Postcond.

ensure (in context of **BANK**)

- ① **old** accounts[i].id → INST.  
 ↳ Account  
 AEA]
- ② (old accounts[i]).id  
 ↳ Account
- ③ (old accounts[i].twin).id  
 ↳ Account
- ④ (old (accounts)[i]).id  
 ↳ A[ACC]
- ⑤ (old accounts twin)[i].id  
 ↳ A[ACC]
- ⑥ (old Current).accounts[i].id  
 ↳ BANK
- ⑦ (old Current twin).accounts[i].id  
 ↳ BANK

## How to cache at runtime?

② old\_c\_twin :=  
 current  
 ⑦ current\_twin :=  
 current.twin



② old\_accs\_i := accounts[i]  
 ③ old\_accs\_i\_twin := accounts[i].twin

① old\_accs\_i\_id := accounts[i].id  
 [23]

→

ACCOUNT	
id	23

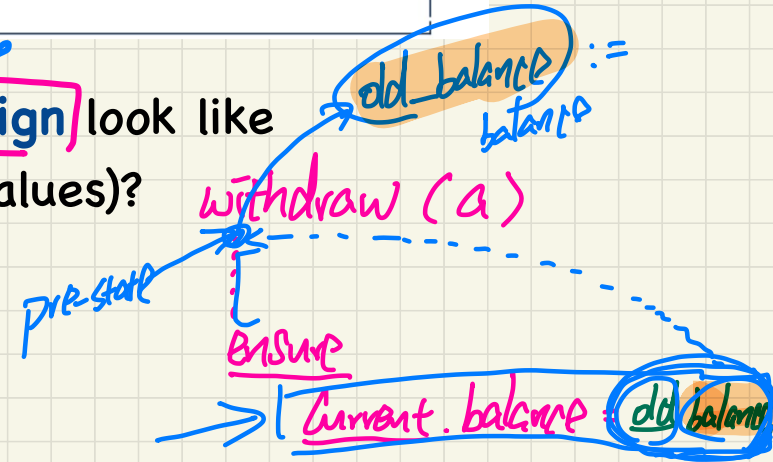
# Revisit: Bank Accounts in Java V5

```
1 public class AccountV5 {  
2     public void withdraw(int amount) throws  
3         WithdrawAmountNegativeException, WithdrawAmountTooLargeException {  
4         int oldBalance = this.balance; ← pre-state  
5         if (amount < 0) { /* negated precondition */  
6             throw new WithdrawAmountNegativeException(); } manual  
7         else if (balance < amount) { /* negated precondition */  
8             throw new WithdrawAmountTooLargeException(); }  
9         else { this.balance = this.balance - amount; }  
10        assert this.getBalance() > 0 : "Invariant: positive balance";  
11        assert this.getBalance() == oldBalance - amount :  
12            "Postcondition: balance deducted"; }  
}
```

post-state

pre-state

How does the corresponding Eiffel design look like  
(with automatic caching of pre-state values)?

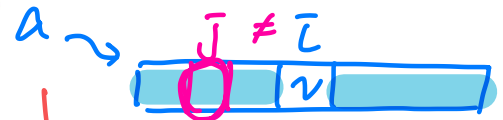


# Use of **old** in **across** Expression in **Postcondition**

```

class LINEAR_CONTAINER
create make
feature -- Attributes
  a: ARRAY[STRING]
feature -- Queries
  count: INTEGER do Result := a.count end
  get (i: INTEGER): STRING do Result := a[i] end
feature -- Commands
  make do create a.make empty end
  update (i: INTEGER; v: STRING)
  do ...
  ensure -- Others Unchanged
    across
      1 .. count (as j)
      all
        j.item /= i implies old get(j.item) == get(j.item)
      end
    end
  end
end
  
```

cache:  
 $get\_j\_item := [get(j.item)]$



For.

$[old \text{ Current.deep-twin}].$   
 $get(j.item)$

→ cursor to int.  
 → pre-state

→ post-state

→  $old \text{ Current.deep-twin}.$   
 $get(j.item)$

Hint: What value will be cached at runtime before executing the implementation of **update**?



```

class BANK
create make
feature
  accounts: ARRAY[ACCOUNT]
  make do create accounts.make_empty end
  account_of (n: STRING): ACCOUNT
    require -- the input name exists
      existing: across accounts is acc some acc.owner ~ n end
      -- not (across accounts is acc all acc.owner /~ n end)
    do ... ensure Result.owner ~ n end
  add (n: STRING)
    require -- the input name does not exist
      non_existing: across accounts is acc all acc.owner /~ n end
      -- not (across accounts is acc some acc.owner ~ n end)
    local new_account: ACCOUNT
    do
      create new_account.make (n)
      accounts.force (new_account, accounts.upper + 1)
    end
end

```

```

class
  ACCOUNT
inherit
  ANY
  redefine is_equal end
create
  make
feature -- Attributes
  owner: STRING
  balance: INTEGER
feature -- Commands
  make (n: STRING)
  do
    owner := n
    balance := 0
  end
end

```

```

deposit(a: INTEGER)
do
  balance := balance + a
  ensure
    balance = old balance + a
  end
end

is_equal(other: ACCOUNT): BOOLEAN
do
  Result :=
    owner ~ other.owner
  and balance = other.balance
end
end

```

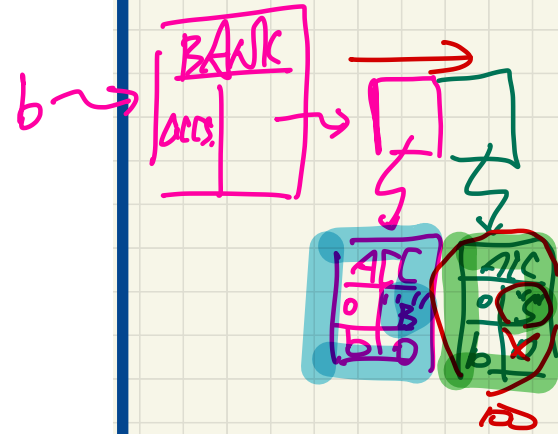
$$\forall x \mid R(x) : P(x)$$

$$\neg (\exists x \mid R(x) \cdot \neg P(x))$$

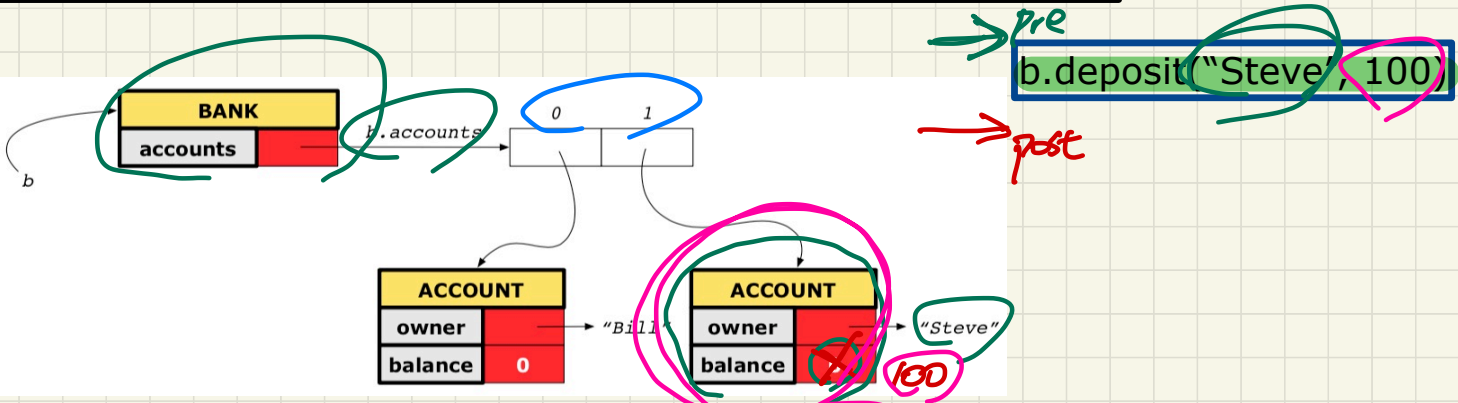
# Unit Test for All 5 Versions

```
class TEST_BANK
  test_bank_deposit_correct_imp_incomplete_contract: BOOLEAN
  local
    b: BANK
  do
    comment("t1: correct imp and incomplete contract")
    create b.make
    b.add ("Bill")
    b.add ("Steve")

    -- deposit 100 dollars to Steve's account
    b.deposit_on_v1 ("Steve", 100)
  Result :=
    b.account_of ("Bill").balance = 0
    and b.account_of ("Steve").balance = 100
  check Result end
end
end
```



# Version 1: Incomplete Contracts, Correct Implementation



→ pre  
**b.deposit("Steve", 100)**  
 → post

```

class BANK
  deposit_on_v1 (n: STRING; a: INTEGER)
  [require across accounts is acc some acc.owner ~ n end]
  local i: INTEGER
  do
    from i := accounts.lower
    until i > accounts.upper
    loop
      if accounts[i].owner ~ n then accounts[i].deposit(a) end
      i := i + 1
    end
  ensure
    num_of_accounts_unchanged:
    accounts.count = old|accounts.count
    balance_of_n_increased:
    Current.account_of(n).balance =
    old|Current.account_of(n).balance + a
  end
end
    
```

② cache:  
accs\_count :=  
 accounts.count  
 imp (over time)

① c-a-a-n-b :=

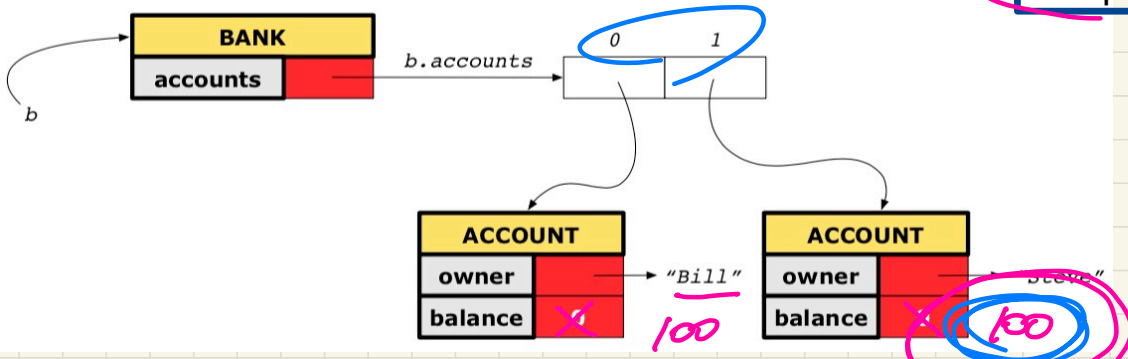
2 = 2 (T)

100 = 0 + 100

100 = 100 (T)

# Version 2: Incomplete Contracts, Wrong Implementation

b.deposit("Steve", 100)



~~Imp. wrong post cond. violation non-satisfactory.~~

no  $\Rightarrow$

cache  
v1 2  
v2 0

correct  
+ account

```

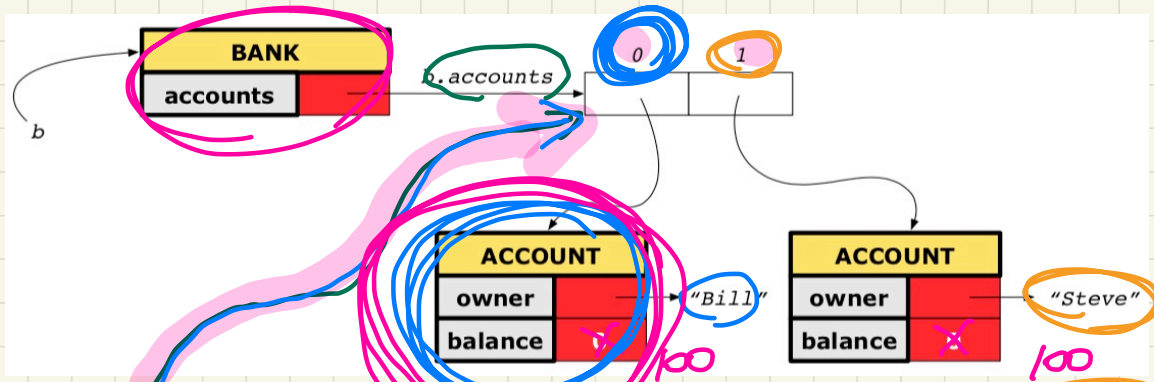
class BANK
  deposit_on_v2 (n: STRING; a: INTEGER)
  [require across accounts is acc some acc.owner ~ n end
  local i: INTEGER
  do ...
  [imp. of version 1, followed by a deposit into 1st account
  [accounts[accounts.lower].deposit(a)
  ensure
  num_of_accounts_unchanged:
  [accounts.count = old[accounts.count]
  balance_of_n_increased:
  [current.account_of(n).balance =
  [old[current.account_of(n).balance] + a
  end
  end
  
```

(T)

100 = 0 + 100

(T)

# Version 3: Complete Contracts (Ref. Copy), Correct Implementation



`b.deposit("Steve", 100)`

cache.  
old\_accs := accounts

$$T \Rightarrow T = \textcircled{T}$$

1st Iteration  
acc.owner /~ n implies acc ~ Current.account\_of(acc.owner)  
Bill Steve

2nd Iteration  
acc.owner /~ n implies acc ~ Current.account\_of(acc.owner)  
Steve Steve

```

class BANK
  deposit_on_v3 (n: STRING; a: INTEGER)
  require across accounts is acc some acc.owner ~ n end
  local i: INTEGER
  do ...
    - imp. of version 1, followed by a deposit into 1st account
    [accounts[accounts.lower].deposit(a)]
  ensure
    num_of_accounts_unchanged: accounts.count = old accounts.count
    balance_of_n_increased:
      Current.account_of(n).balance =
        old Current.account_of(n).balance + a
  ensure
    across old accounts is acc
    all
      acc.owner /~ n implies acc ~ Current.account_of(acc.owner)
    end
  end
end
  
```

# Use of **across** in **Postcondition**

$$\left. \begin{aligned} T \Rightarrow P &\equiv P. \\ F \Rightarrow P &\equiv T \end{aligned} \right\}$$

```

across old (accounts) is acc
all
  acc.owner /~ n
implies
  acc ~ Current.account_of (acc.owner)
end
  
```

Annotations:
 

- old** (accounts) is **acc**: pre-state
- acc: pre-state "value"
- ACCOUNT: for each amount
- Current**.account\_of (acc.owner): post-state
- acc: ACC
- Account\_of: post-state
- acc.owner /~ n: pre-state

## For each iteration:

**Case 1:** **acc.owner** is **not** **n** *Step*

$\text{acc.owner} / \sim n \text{ implies } \text{acc} \sim \text{Current.account\_of} (\text{acc.owner})$

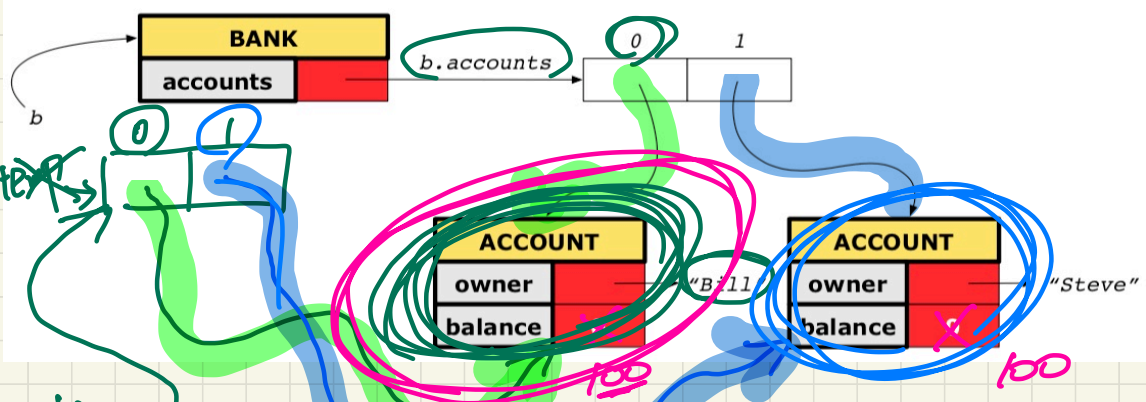
**Case 2:** **acc.owner** is **n** *Step*

$\text{acc.owner} / \sim n \text{ implies } \text{acc} \sim \text{Current.account\_of} (\text{acc.owner})$

Additional notes:
 

- Case 1** and **Case 2** are circled in orange.
- Case 1** has a note "p.s.v. Bill" pointing to the **n**.
- Case 2** has a note "Bill" pointing to the **n**.
- A circled **T** is connected to the **implies** part of Case 2.
- The **implies** part of Case 2 is circled in pink.
- The **acc** and **Current** in Case 2 are circled in pink.

# Version 4: Complete Contracts (Shallow Copy), Correct Implementation



`b.deposit("Steve", 100)`

`temp[0] := b.accounts[0]`  
`temp[1] := b.accounts[1]`

cache  
 old\_accs\_twin

$T \Rightarrow T$   
 $T$   
 $T$

1st Iteration

`acc.owner /~ n` implies `acc ~ Current.account_of(acc.owner)`  
 Bill Steve  
 Bill Steve

2nd Iteration I

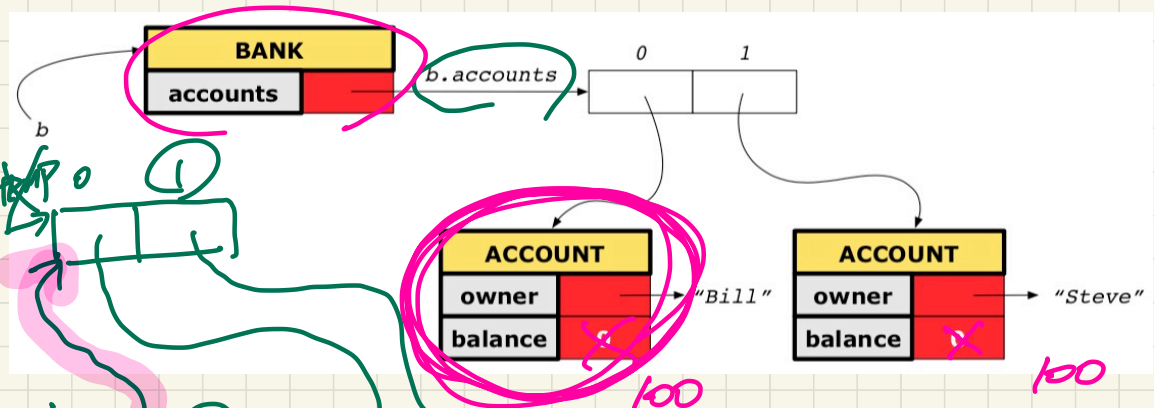
`acc.owner /~ n` implies `acc ~ Current.account_of(acc.owner)`  
 Steve Steve

```

class BANK
  deposit_on_v4 (s: STRING; a: INTEGER)
  require across accounts is acc some acc.owner ~ n end
  local i: INTEGER
  do ...
    -- imp. of version 1, followed by a deposit into 1st account
    accounts[accounts.lower].deposit(a)
  ensure
    num_of_accounts_unchanged: accounts.count = old accounts.count
    balance_of_n_increased:
      Current.account_of(n).balance =
        old Current.account_of(n).balance + a
    others_unchanged:
      across old accounts.twin is acc
      all
        acc.owner /~ n implies acc ~ Current.account_of(acc.owner)
      end
  end
end
    
```



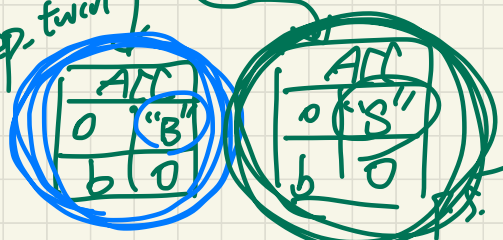
# Version 5: Complete Contracts (Deep Copy), Correct Implementation



`b.deposit("Steve", 100)`

`temp[0] := b.accounts[0].dt`  
`temp[i] := b.accounts[i].dt`

Cache  
`o.accounts.dt :=`  
 accounts: deep twin



```

class BANK
  deposit_on_v5 (n: STRING; a: INTEGER)
  [ require across accounts is acc some acc.owner ~ n end
  local i: INTEGER
  do ...
  -- imp. of version 1, followed by a deposit into 1st account
  accounts[accounts.lower].deposit(a)
  ensure
    num_of_accounts_unchanged: accounts.count = old accounts.count
    balance_of_n_increased:
      Current.account_of(n).balance =
        old Current.account_of(n).balance + a
    others_unchanged:
      across old accounts.deep_twin is acc
      all
        acc.owner ~ n implies acc ~ Current.account_of(acc.owner)
      end
  end
end
    
```

appropriate wrong imp  
 Post cond.  
 ⇒ validation

1st Iteration T

`acc.owner ~ n implies acc ~ Current.account_of(acc.owner)`  
 Bill Steve  
 F T

2nd Iteration F

`acc.owner ~ n implies acc ~ Current.account_of(acc.owner)`  
 Steve Steve  
 T T

# Complete Postcondition: Exercise



Consider the query *account\_of* (*n*: *STRING*) of *BANK*.

How do we specify (part of) its postcondition to **assert that the state of the bank remains unchanged:**

- `accounts = old accounts`
- `accounts = old accounts.twin`
- `accounts = old accounts.deep_twin`
- `accounts ~ old accounts`
- `accounts ~ old accounts.twin`
- `accounts ~ old accounts.deep_twin`

